Comment 01 on ECCC TR97-006

A correction to:

Parameterized Parallel Complexity

ECCC TR97-006

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In the fourth section of [1], we study a possible connection between the classical complexity class NC and the parameterized classes FPP and PNC. In particular, we claim the existence of a parameterized problem belonging to FPT such that all its slices are P-complete. By using such problem we can show that if NC \neq P, then no FPT-hard problem (both considering FPP-reductions and PNC-reductions) can have all slices included in NC.

Unfortunately, a crucial proof in this section is wrong. We claimed that each slice of the parameterized LONGEST PATH problem is P-complete by showing a classical logspace reduction from the MONOTONE CIRCUIT VALUE problem. As pointed out by H. Fernau, K-J. Lange and R. Niedermeier [3], the claimed reduction does not hold, because the obtained graph could have additional unwanted paths due to the lacking of a "copy" operation beside the tradional logic operators.

Actually, parameterized tractable problems whose slices are P-complete really exist. Miyano [2] proved that almost all slices of the LEXICOGRAPHICALLY FIRST MAXIMAL k-CYCLE-FREE EDGE-INDUCED SUBGRAPH problem are P-complete. The instance of such problem consists of an undirected graph G = (V, E) with a linear ordering on the edges and a designate edge $e \in E$; the question is whether e belongs to the lexicographically-first maximal edge-induced subgraph which does not contain a k-cycle (k being the parameter). Fernau, Lange and Niedermeier [3] showed that all "lexicographically first maximal Π_k edge-induced subgraph" problems characterized by a FPT-checkable graph property Π_k belong to FPT. Indeed, a simple greedy strategy can solve it.

However, we can also exhibit far simpler parameterized tractable problems whose slices are all P-complete. Let us consider for example the WEIGHTED CIRCUIT VALUE problem WCV: its instance consists of the description of a logical decision circuit C and of an input word w; the parameter k is the Hamming weight of w, and the question is whether C accepts w. Since the classical CIRCUIT VALUE problem CV is polynomially solvable, the weighted parameterized

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version is in FPT. Moreover, each slice WCV_k is P-complete. Indeed, consider that for each binary word v it is possible to construct with a parallel algorithm and in constant time a simple circuit C_v which transforms the word $w = 1^k$ into v. The circuit obtained by the joining of C_v and C accepts w if and only if C accepts v.

References

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